This paper empirically demonstrates the possibility of setting up an optimal pollution tax under imperfect markets and international trade in a domestic economy. The model illustrates a situation of partial equilibrium characterized by imperfect competition among domestic producers, where the domestic good is used as an alternative for an imported polluting commodity. In this paper, we bring in the possibility that the domestic firms can introduce innovative ideas through investment in R&D. The result shows that the optimal pollution tax under domestic economic distortions is a function of a ‘domestic production effect’ and a ‘pollution effect’. The paper concludes that when the firms execute R&D expenditures, the optimal policy adds an ‘innovative effect’, which captures the change in welfare coming from a reduction in total costs and this lead our results to a win-win situation.

Contribution/Originality: The paper contributes in the existing literature by illustrating the case of partial equilibrium characterized by imperfect market among domestic producers. It introduces innovative ideas through the incorporation of investment in research and development. The paper concludes that under a win – win situation optimal environmental policy represent a policy tax.

1. INTRODUCTION

Arguably, optimal tax pollution is the sum of domestic production effect and a pollution effect where one firm represents a decrease in social welfare due to a reduction in pollution damage while the second constitutes an increase in social welfare as a result of reduction in pollution damage. Though, as essential as Air Transport services in modern economics its negative impact are felt globally (Solarin and Bradford, 2014; Porter, 2015) some of the impact of aviation transport on climate change stems from Co2, NOX and contrails and cirrus clouds, Co2 emission as the major impact (Corden, 2013) Although most externalities that originates from transport have a negative impact, there may be also positive effect (Basso, 2008; Kennedy, 2014)

The economic literature on the link between optimal pollution tax and Air transport services becomes very scanty (Ulph, 2014) and the available ones treat environmental policies impact on international trade by means of large simplifications of reality for which their conclusion could lead policy makers to a misunderstanding of the time tradeoff between domestic and international competitivenes. This emphasizes the need to work on partial equilibrium model in order to understand this kind of tradeoff.
Against this background, this study aims at establishing a theoretical foundation that will give us the impetus to understand the characteristics of environmental policy options. The remainder of this paper is structured as follows. Section 2 explains the basic model by establishing the optimal pollution policy that can maximizes the social welfare. Section 3 sets out the pollution tax level when firms carry out endogenous R and D investments. The last section provides a summary and suggests some directive for further research.

2. THE MODEL

We place a two-stage game with two players to solve our regulation problem. Hence, working backward from the firms’ decisions to the government’s tax decision, in the second stage, the producers choose their outputs and abatement levels under a Nash-Cournot behavioural assumption and, in the first stage, the government sets the tax on pollution to maximize social welfare, recognizing that both equilibrium behaviour of firms and the imports of the substitute commodity depend on the tax.

Corden (2013) and Conrad (2009) noted that in the present context of a small open economy, the pollution (production) tax represents a first-best policy. However, we rule out the use of industrial policy on the assumption that environmental policy is politically more feasible than the previous one. Moreover, we assume that there is no interaction with other sectors of the economy, that the economy acts as a net-importer of the foreign good and that the factor prices are given. First, the paper focuses on with the effects of a specific pollution tax on emissions in a static context (i.e., a particular period of time), in which market structure, cost conditions and entry barriers are given. Second, we focus on industries where domestic firms sell in domestic markets but do not export the product. Third, working in a first-best policy leaves out the possibility of trade balance problems in the long run (i.e., the internationalization of the environmental damage should improve the trade patterns and, therefore, the gains from trade). Finally, we work in a complete information model, where the government is assumed to know the demand structure of the firms’ output as well as their cost functions. Thus, it correctly anticipates the domestic firms’ output decisions given the imposed emission tax.

2.1. Domestic Firms

The industry of the domestic good, t, consists of n identical firms, where the producing process generates a pollutant whose quantity depends on the level of production and abatement activities. Therefore, we can express the cost function for the firm as Cj(tj, aj), where tj and aj are the levels of production and abatement effort respectively. Also, we assume that Cj is increasing and strictly convex in its arguments, i.e., Cj′ > 0, Cj″ > 0 Cj′′t > 0, and Cj′′a > 0 for all tj and aj, and that the level of emissions, ej, takes the following functional form: ej = el(tj, aj), with el′ > 0, el′′ < 0, el′′′t > 0, and el′′′a > 0. Then, if Pj(t, y, I) denotes the inverse demand function for t, with y and I representing the imported good and the monetary income respectively, in the second-stage game the representative firm chooses its output, tj, and abatement, aj, levels, recognizing that the rivals’ output and abatement levels as well as the environmental tax placed by the government, r, are given, to maximize the following profit function:

\[ n^i (t^i, a^i) = P^i (t, y, I) - Cj(tj, aj) - re(tj, aj), j = 1, \ldots, n, \]  

which yields the first-order conditions

\[ \frac{\partial P^i(t, y, I)}{\partial t} - Cj'(tj, aj) - re'(tj, aj) = 0 \]  

(2a)

\[ -Cj''(tj, aj) - re''(tj, aj) = 0. \]  

(2b)

Aggregating, taking into account that the aggregate level of production of the domestic industry, t, is equal to t = nt; of abatement, a, is equal to a = na; and of emissions, e, is equal to e = ne; we can express the first-order conditions for the maximization of the profits at the industry level as:

\[ P(t, y, I) - (Cj(t, a) + re(a, a)) = -\frac{1}{n} \lambda \]  

(3a)
Expression (3a) is a variant of the well-known equilibrium condition in Cournot models, stating that the Lerner index of any individual firm must be equal to that firm’s market share divided by the absolute value of total-market-demand elasticity, whereas condition (3b) implies that firms abate pollution to the point where their marginal cost of reducing emissions equals the pollution tax.

2.2. Market Equilibrium

Using (3a), we can express the equilibrium output for the domestic market

\[
t = - \left[ P_t(t, y, I) - (C_{t\alpha} + r e) \right] \frac{n}{V_t} \tag{4}
\]

Therefore, from (4), the response of the domestic output to a change in r is given by

\[
\frac{\partial t}{\partial r} = \frac{e + (C_{t\alpha} + r e) \partial a / \partial r}{V_t \left[ \frac{r_{\alpha\tau}}{n} \left( C_{t\tau} + r e \right) + \frac{r_{e\tau}}{V_t} \left( P_t - (C_t + r e) \right) \right]} \tag{5}
\]

Note that as \( e_{\alpha\tau} < 0 \), the sign of the second term in the numerator is determined by the effect of an increase in the level of abatement efforts on production costs, \( C_{t\alpha} \), which could be positive, zero, or negative, depending on the relation between these activities. In other words, the degree of complementarity between these processes will define the sign of the cross-partial derivative. Also, in the case of linear demand functions, \( V_{t\tau} = 0 \), the third term of the denominator, disappears from the expression. However, since \( \frac{\partial a}{\partial r} > 0 \) and primary effects (first derivatives) generally dominate secondary effects (second derivatives), the sign of (5) is assumed negative.

2.3. Social Welfare and Optimal Policy

From the above, we can express the government revenues coming from the pollution tax on domestic emissions as \( r e \). Therefore, if \( D(e) \) denotes the environmental damage resulting from any aggregate level of pollution in monetary terms, it is possible to define the social welfare function, \( SW \), as the sum of (i) the consumer surpluses, (ii) the domestic industry profits, and (iii) the government revenues, less (iv) the pollution damage.

\[
SW = \left( \int_0^{nT} P_t(t, y, I) dt - P_t t^T \right) + \left( \int_0^{y_{\alpha\tau}} \left( P_Y Y + \pi(t, a) + r e - D(e) \right) \right) \tag{6}
\]

Where \( P_t(t, y, I) \) denotes the inverse demand function for \( y \), \( P_t^1 \) and \( P_t^0 \) represent the price of the domestic and imported good, respectively, and \( D(e) \) is assumed to be increasing and strictly convex, i.e., \( D_e > 0 \) and \( D_{ee} > 0 \) for all \( e \). This specification of aggregate social welfare avoids the issue of income distribution effects by weighting each welfare component equally; a way to modify it is to introduce an alternative weighting system. Hence, replacing in \( \pi(t, a) \) and \( e \), we can rewrite (6) as...
This provides a simple interpretation of the social welfare as the total benefits from consuming t and y less the private cost of producing t, the social cost of acquiring y (its domestic or international price), and the loss in consumer utility generated by the level of pollution. Then, turning to the analysis of the pollution tax that maximizes the social welfare, we find that in the first-stage game the government chooses the value of r that maximizes (7), recognizing that y is a function of t and that t depends on r. From (7), the effect on SW of a small change in r is given by

$$\frac{\partial SW}{\partial r} = \left( (Px - Ct) - Deel \right) \frac{\partial t}{\partial r} - \left( Ca + Deel \alpha \right) \frac{\partial \alpha}{\partial r}$$  \hspace{1cm} (8)

Then, substituting in (8) for (3a) and (3b), we obtain the result that $\frac{\partial SW}{\partial r} = 0$ when $r = r^*$, where

$$r^* = \frac{ve}{h} \frac{\partial e}{\partial r} \frac{1}{h} + De$$  \hspace{1cm} (9)

with

$$h = e, \quad \frac{\partial e}{\partial r} + e \alpha \frac{\partial \alpha}{\partial r} \frac{1}{h} < 0$$

the intuition behind this expression is as follows: The first term denotes the ‘domestic production effect’ and represents a decrease in the welfare of the society. That is, as t is a good whose marginal benefit to consumers ($P_t$) exceeds its marginal cost (apart from the pollution cost), a higher r decreases the amount of sales of the domestic firms and, therefore, the social welfare. On the other hand, the second term stands for the ‘pollution effect’ and constitutes an improvement in social welfare. Here, a higher r results in a lower level of emissions, which improves the social welfare because of the decrease in the pollution damage. Also, note that as y is a negative function t, $\frac{\partial y}{\partial t} < 0$, a drop in the sales of the domestic firms augments the amount imported of the good y. Therefore depending on whether or not the ‘pollution effect’ exceeds the ‘domestic production effect’, the optimal policy consists of a tax-cum-subsidy on pollution.

3. ENDOGENOUS R & D INVESTMENTS

The model described above provides a tractable framework to allow for the possibility of private actions to counteract the environmental tax effects. Here, we assume that the domestic producers can neutralize such effects through the introduction of some innovation offsets, where the strategic variable for the firms is the investment in R&D. Hence, we need to focus on a three-stage game, where in the second-stage the producers choose their R&D expenditures required to employ a particular technology, and in the third-stage they choose their outputs and abatement levels. Hence, assuming that the total, average, and marginal costs are decreasing and convex in innovation expenditures, O, and that the new technology reduces the production as well as the abatement costs, we
can express the firm’s total cost function as \( C_j(t_j, a_j, \Omega_j) \), with \( C_{t\Omega} < 0 \) and \( C_{\Omega\Omega} > 0 \) for all \( \Omega \). Now, at the third-stage game the \( j \)th firm chooses its own output, \( t_j \), and abatement level, \( a_j \), recognizing that the emission tax, \( r \), set by the government in stage one, the level of \( \Omega \) set in stage two, \( \Omega \), and the output and abatement level of its rivals are given. This leads to the following first-order conditions for the domestic industry:

\[
P(t, y, l) - (C(t, a, \Omega*) + re(t, a)) = -t \frac{Vt}{n} \quad (10a)
\]

\[
r = -\frac{Ca(t, a, \Omega*)}{ea(x,a)} \quad (10b)
\]

In the second-stage game, the representative firm maximizes its profits with respect to \( \Omega_j \), assuming that the rivals’ expenditures on R&D are given. However, it figures out that its output and abatement level and the rivals’ output and abatement level in the next stage depend on \( \Omega \). Therefore, it chooses \( \Omega \) to maximize

\[
\pi_j(t_j(\Omega_j), a_j(\Omega_j), \Omega_j) = P(t(\Omega_j), y, I)t_j(\Omega_j) - C_j(t_j(\Omega_j), a_j(\Omega_j), \Omega_j) - Re_j(t_j(\Omega_j), a_j(\Omega_j), \Omega_j)
\]

Where the first-order condition at the industry level is given by

\[
P = (C_t + Ca \frac{\partial a}{\partial \Omega} + r (et + ea \frac{\partial a}{\partial \Omega}) + \frac{Cx + Ca \frac{\partial a}{\partial \Omega}}{\partial \Omega} = -t \frac{Vt}{n} \quad (12)
\]

Where \( \Omega \) and \( C_\Omega \) are the level of innovation expenditures and the innovation marginal cost for the domestic industry respectively. Furthermore, the third term in the brackets represents the change in the market power of the domestic firms, an increase in \( \Omega \) decreases the cost of production per unit of output, which, since \( \frac{\partial t}{\partial \Omega} > 0 \), increases the sales of \( t \).

Since the derivation of an optimal value of innovation, \( \Omega^* \), in explicit form is impossible, we can obtain additional insights by taking the second-order condition for a maximum. Then, from (12) we obtain

\[
\frac{\partial C_\Omega}{\partial \Omega} > (Vt \frac{1+\Omega}{n} + t \frac{Vt}{n})
\]

\[
-\left[ Ctt + 2Cta \frac{\partial a}{\partial \Omega} + Caa \left( \frac{\partial a}{\partial \Omega} \right)^2 + \frac{Cwa + Ca\frac{\partial a}{\partial \Omega}}{\partial \Omega} \right] \frac{\partial a}{\partial t} \quad (13)
\]

Where \( \frac{\partial }{\partial \Omega} \) is positive and \( C_{t\Omega} \) and \( C_{a\Omega} \) are negative by definition. Thus, as the terms in brackets above denote the demand and supply sides of the market, the effect of a change in \( \Omega \) on the market power of the domestic industry will be greater under linear demand functions (i.e., \( V_t = 0 \)) and complementary activities, \( C_{ta} > 0 \).

Finally, in the first-stage game, the government maximizes \( SW(r) \) recognizing that \( t, y \) and \( \Omega \) all depend on \( r \). Therefore, the first-order condition for the government problem is
\[ 0 = ((P_t - C_t) - D_e t) \left( \frac{\partial t}{\partial r} + \frac{\partial t}{\partial \theta} \frac{\partial \theta}{\partial r} \right) \]

\[ - (C + D_e a) \left( \frac{\partial t}{\partial r} + \frac{\partial t}{\partial \theta} \frac{\partial \theta}{\partial r} \right) - C_0 \frac{\partial \theta}{\partial r} \]

(14)

With \( \frac{\partial \theta}{\partial r} > 0 \). Hence, using (10a) and (10b), the optimal tax pollution \( r^* \), can be written as

\[ r^* = t \left( \frac{\partial t}{\partial r} + \frac{\partial t}{\partial \theta} \frac{\partial \theta}{\partial r} \right) - C_0 \frac{\partial \theta}{\partial r} \frac{1}{p} + D_e \]

(15)

with

\[ p = et \left( \frac{\partial t}{\partial r} + \frac{\partial t}{\partial \theta} \frac{\partial \theta}{\partial r} \right) + e_a \left( \frac{\partial a}{\partial r} + \frac{\partial a}{\partial \theta} \frac{\partial \theta}{\partial r} \right) \]

Comparing (9) with (15), we observe that the introduction of innovation offsets generate some distinctive characteristics in the expression for \( r \). Now, it is possible to reverse the conclusion that under non-competitive conditions the optimal policy should be a tax-cum-subsidy on pollution. To see this, note that when such offsets are added, the signs of the numerator and denominator of the ‘domestic production effect’ are undetermined, which implies the possibility that it can turn positive? In other words, this will happen when

\[ p < 0 < \left( \frac{\partial t}{\partial r} + \frac{\partial t}{\partial \theta} \frac{\partial \theta}{\partial r} \right) \]

or

\[ \frac{\partial \theta}{\partial r} \left( \frac{\partial t}{\partial r} + \frac{\partial t}{\partial \theta} \frac{\partial \theta}{\partial r} \right) \left( \frac{\partial t}{\partial r} + \frac{\partial t}{\partial \theta} \frac{\partial \theta}{\partial r} \right) \]

With

\[ \left( \frac{\partial t}{\partial r} + \frac{\partial t}{\partial \theta} \frac{\partial \theta}{\partial r} \right) > 0 \]

The rationale behind this result is as follows: when the indirect effect generated by the innovation process surpasses the direct effect of \( r \) on \( t \) and the denominator still remains negative, since the abatement effect dominates the production effect of \( r \) on \( e \), the introduction of innovation offsets not only increases the sales of \( t \) but also decreases the level of emissions, which, therefore, improves the social welfare. Also, note that as the domestic sales of \( t \) increase, there will be a drop in the quantity imported of good \( y \). In contrast, if the direct effect dominates the indirect effect of \( r \) on \( t \) (i.e., \( p < 0 \) with \( \left( \frac{\partial t}{\partial r} + \frac{\partial t}{\partial \theta} \frac{\partial \theta}{\partial r} \right) < 0 \)), the ‘domestic production effect’ maintains its negative sign. In addition, the second term in (15) describes what we call the ‘innovation effect’: an increase in \( r \) diminishes the production costs, which is welfare increasing when the new equilibrium for \( t \) is associated with a lower level of emissions, \( p < 0 \), or welfare decreasing when the contrary happens, \( p > 0 \). Hence, we observe that under a win-win situation (i.e., when the firms can reduce their emissions level and increase their domestic sales), the optimal policy
represents a tax on pollution and has a higher level than the previous one (without innovation offsets), i.e., \( r^{**} > r^* \), with \( r^{**} > 0 \), and \( r^* > = < 0 \). Otherwise, if the innovation offsets are positively correlated with higher emissions (i.e., \( p > 0 \)), we obtain that \( r^{**} \) could be lower or greater than \( r^* \).

4. CONCLUSIONS

This paper focuses on the design of optimal environmental policy when non-competitive conditions exist in a small economy. To accomplish this, we work in a two-good partial equilibrium model, where one of the goods is imported from a foreign country. As the preceding analysis made clear, the optimal pollution policy under domestic distortions can be decomposed into a ‘domestic production effect’, which describes the change in welfare coming from a variation in the level of domestic firms’ sales, and a ‘pollution effect’, capturing the change in welfare coming from a variation in pollution damage. Furthermore, since these two effects have opposite signs, the optimal policy will be a tax-cum-subsidy on pollution, depending on whether or not the ‘pollution effect’ dominates the ‘domestic production effect’.

Interesting highlights appear when the firms have the possibility of introducing innovation offsets through their investment in R&D. In this case, the optimal pollution tax adds an ‘innovation effect’, which captures the change in welfare coming from a decrease in production costs. From the analysis, its effect on welfare will depend on whether the new equilibrium (after the tax) for the domestic industry is associated with a higher or lower level of emissions, creating the possibility that we can obtain a win- win situation when the innovation offsets generate more abatement than emissions and the domestic firms increase their sales. Finally, we conclude that only under a win-win situation does the optimal environmental policy represent a tax and it is higher than the previous one (without innovation offsets). Otherwise, a comparison between them is impossible.

There are many additional areas of research that could be pursued. A natural extension would be to admit the presence of foreign direct investment in the form of local production of the imported good. Another development would be to introduce stochastic elements.

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